

# 3D Mask Simulation and Lithographic Imaging using Physics-Informed Neural Networks (PINN)

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# Author

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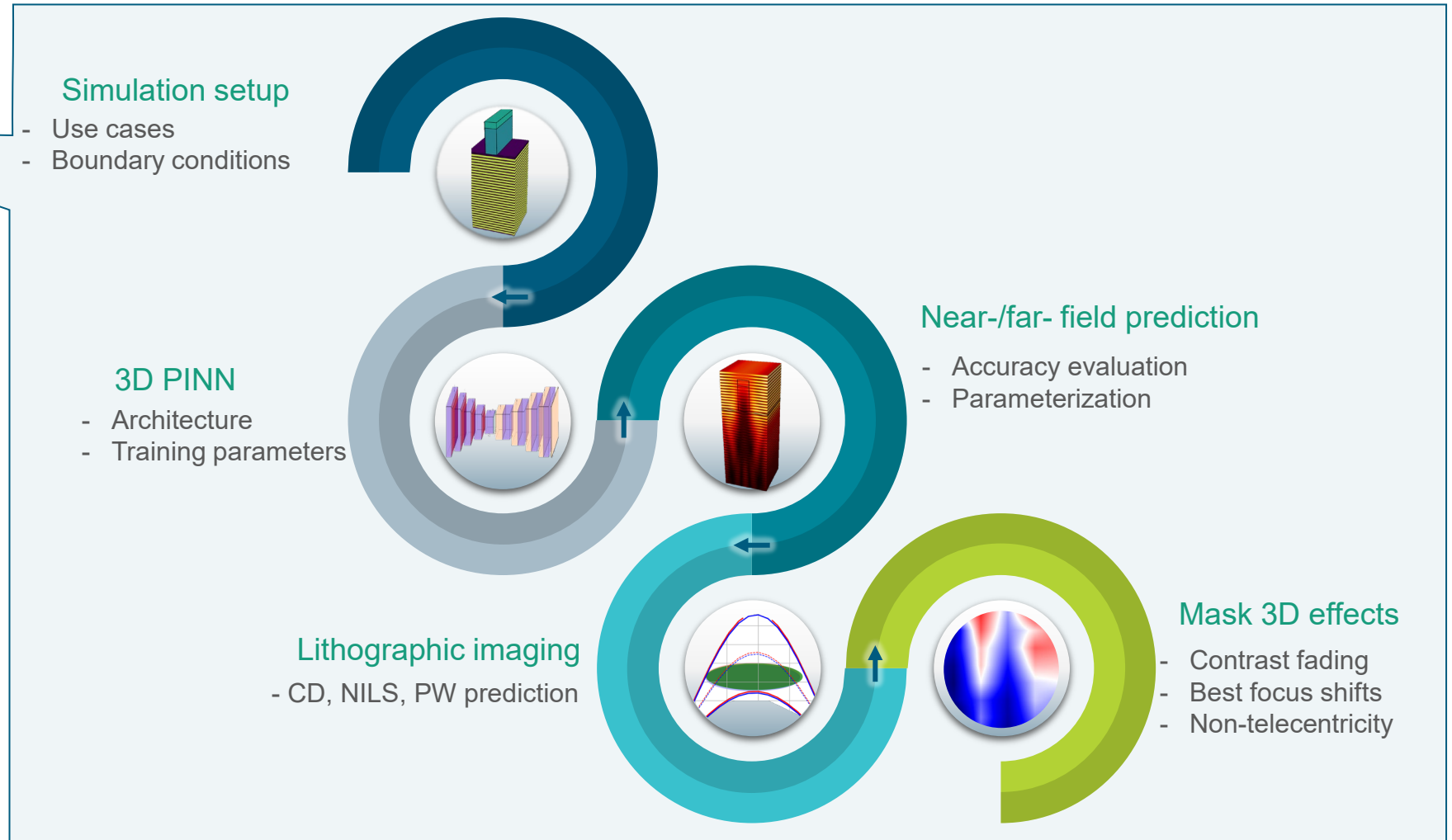
- 2019 - 2022     **M.Sc., Advanced Optical Technologies**, Friedrich-Alexander-Universität Erlangen-Nürnberg, Germany.  
Thesis title: *3D mask defect and repair based on SEM images.*
- 2022 - present     **Ph.D., Computational Lithography & AI-Augmented Simulation Groups**, Fraunhofer IISB, Germany.  
Thesis topic: *Physics Informed Neural Networks (PINNs) for modeling of light diffraction from EUV masks and optical metasurfaces.*

# Outline

**Part 1:** Introduction and motivation

**Part 2:** Workflow

**Part 3:** Summary and Outlook



Part 1

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# Introduction and motivation

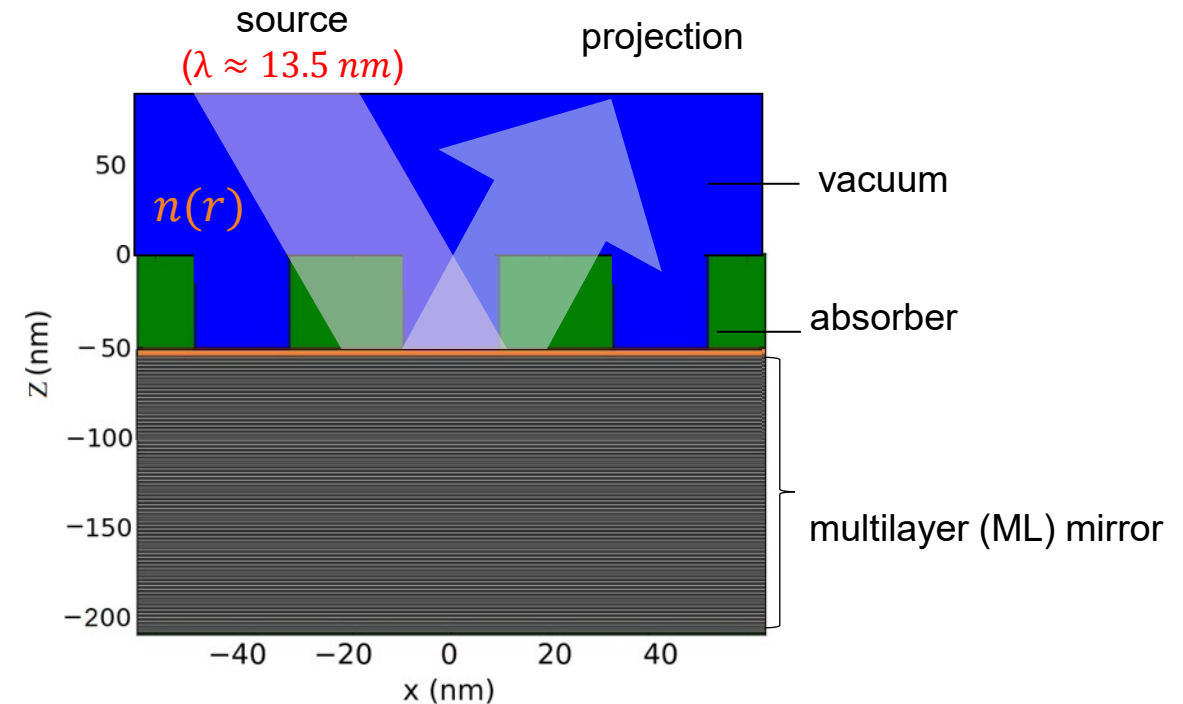
# Introduction

## Rigorous electromagnetic (EM) simulation in EUVL:

- Highly required for **accurate simulation of EUV imaging** and design and optimization of lithographic manufacturing processes.
- Involves solving the scattering problem through numerical approximations domain **Maxwell's equation** in the scalar form:

$$\nabla^2 E(r) + n^2(r)k_0^2 E(r) = 0$$

- Challenges:
  - modeling with the required **accuracy**.
  - modeling of **larger mask areas** with design-relevant layouts.
  - **fast** modeling.



# Motivation

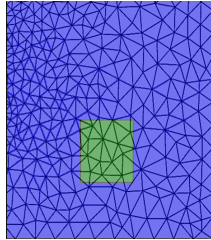
## Alternative to traditional solutions

(i) Traditional numerical solvers (e.g., FEM<sup>1</sup>, FDTD<sup>2</sup>, RCWA<sup>3</sup>):

**Idea:** numerical techniques to iteratively solve EM simulations.

Computation time/memory amount increases for:

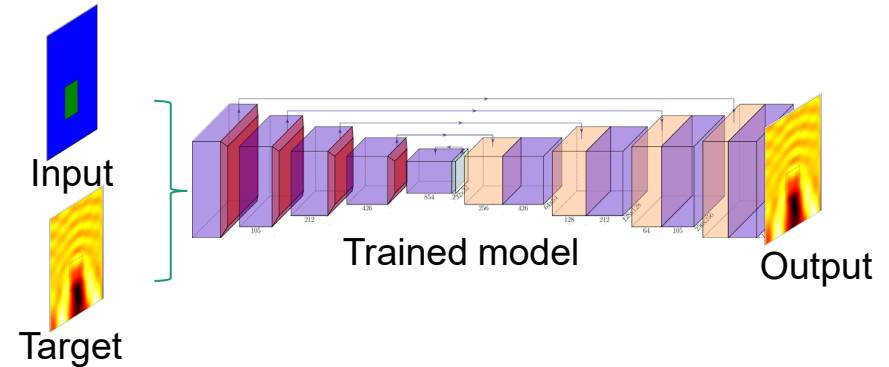
- complex physical problems.
- modeling of larger mask areas with design-relevant layouts.
- high resolution/discretization.



(ii) Data-driven deep learning (e.g., GAN<sup>4</sup>, CNN<sup>5</sup>):

**Idea:** learns a correlation between input and output.

- Supervised based on a huge amount of expensive rigorously simulated or measured data.
- Valuable information carried by physics is ignored.



**Motivation:** explore the potential of (iii) physics-informed neural networks (PINN) for addressing complex optical problems in the field of EUV lithography to overcome aforementioned constraints.

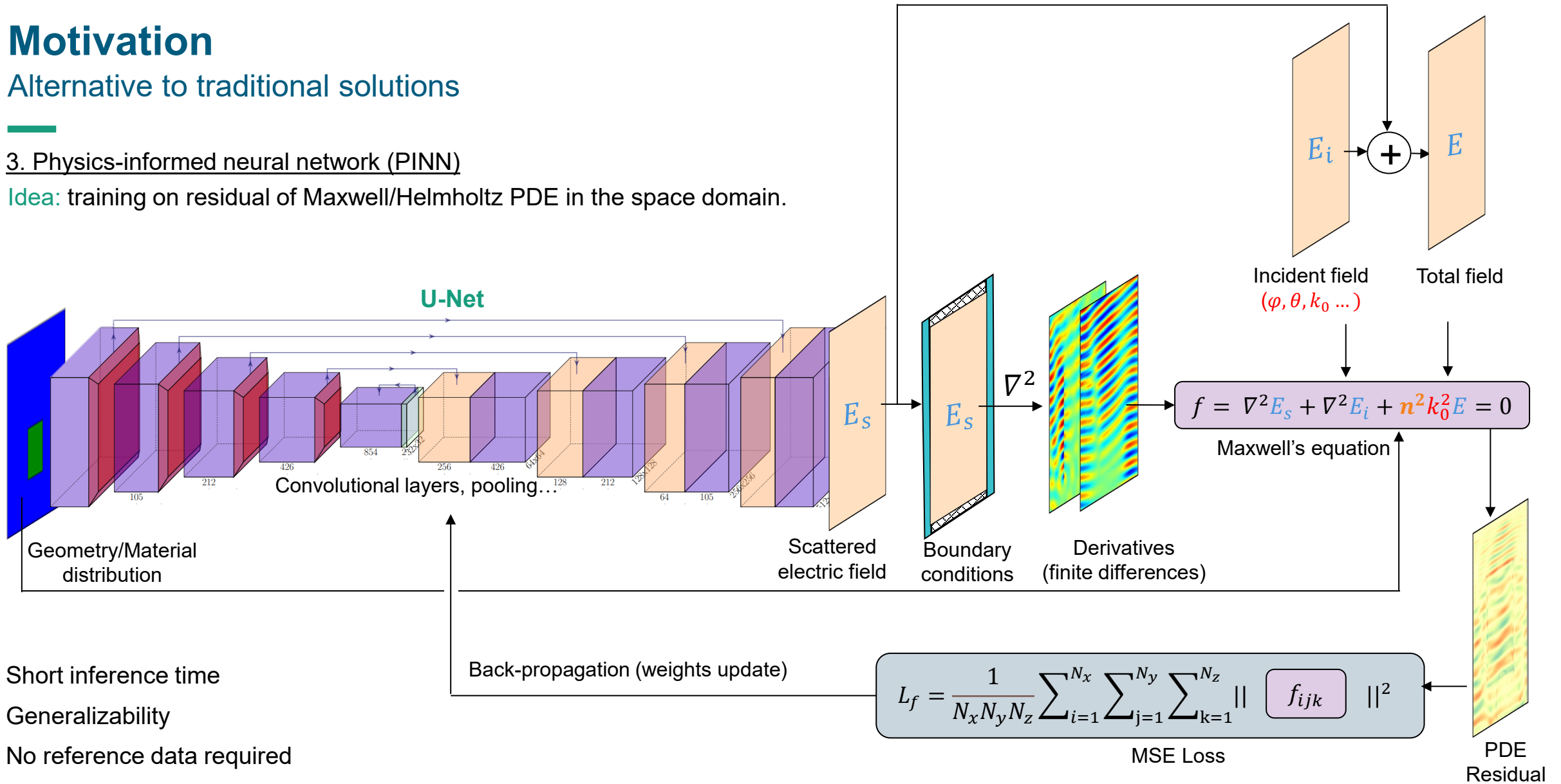
1 - Finite element method  
2 - Finite-difference time-domain method  
3 - Rigorous coupled-wave analysis  
4 - Generative adversarial network  
5 - Convolutional neural network

# Motivation

## Alternative to traditional solutions

### 3. Physics-informed neural network (PINN)

Idea: training on residual of Maxwell/Helmholtz PDE in the space domain.



Part 2

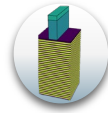
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# Workflow

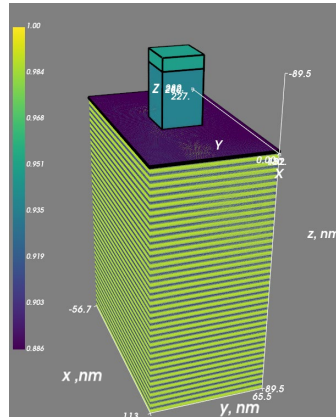


# Simulation setup

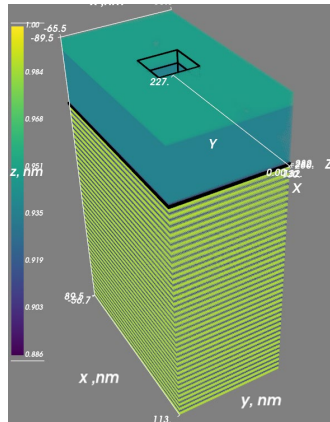
## Use cases



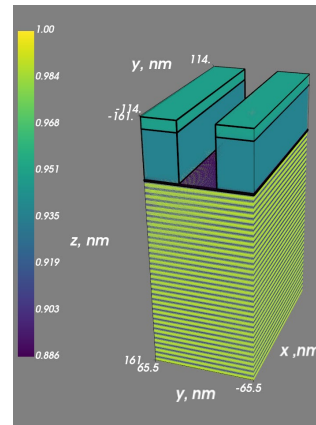
### Different feature types



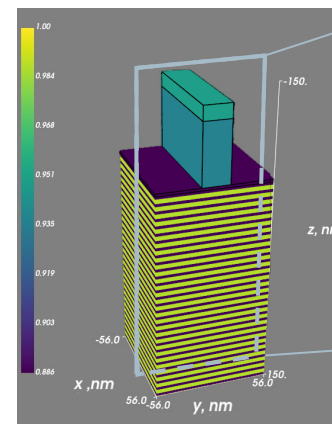
Pillar



Contact hole

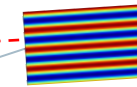


Space

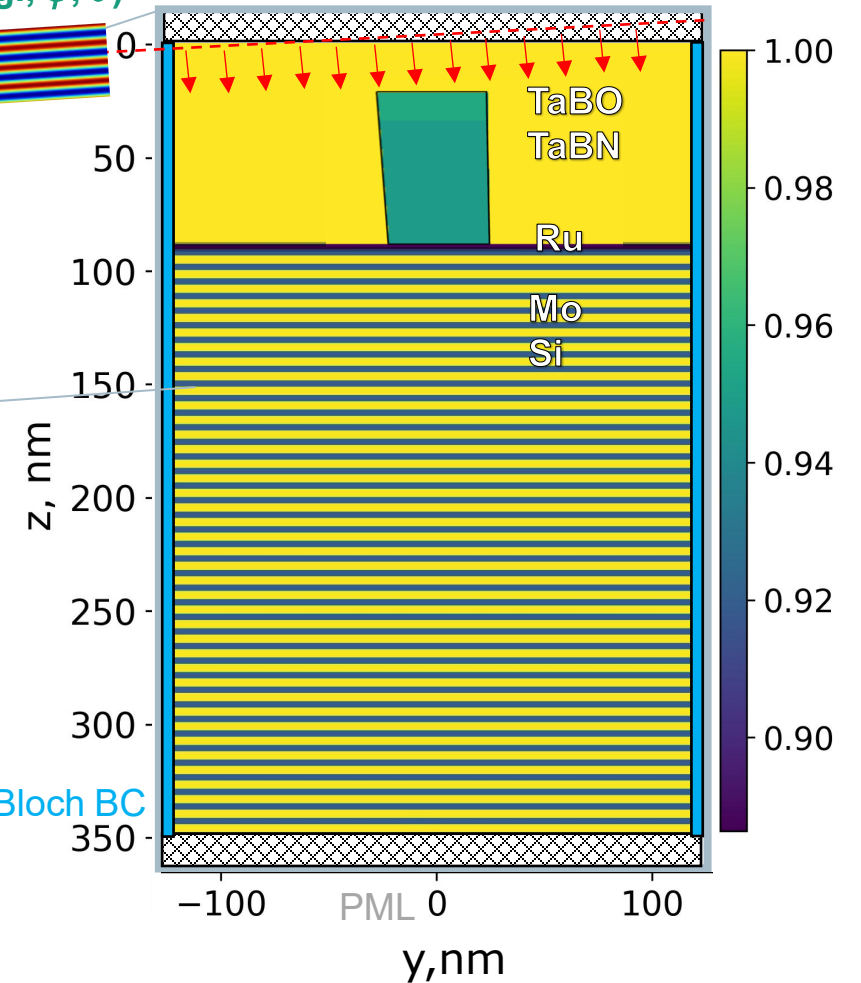


Line

Different illumination directions (e.g.,  $\varphi$ ,  $\theta$ )



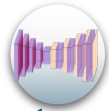
Different mask geometries (e.g., SWA)



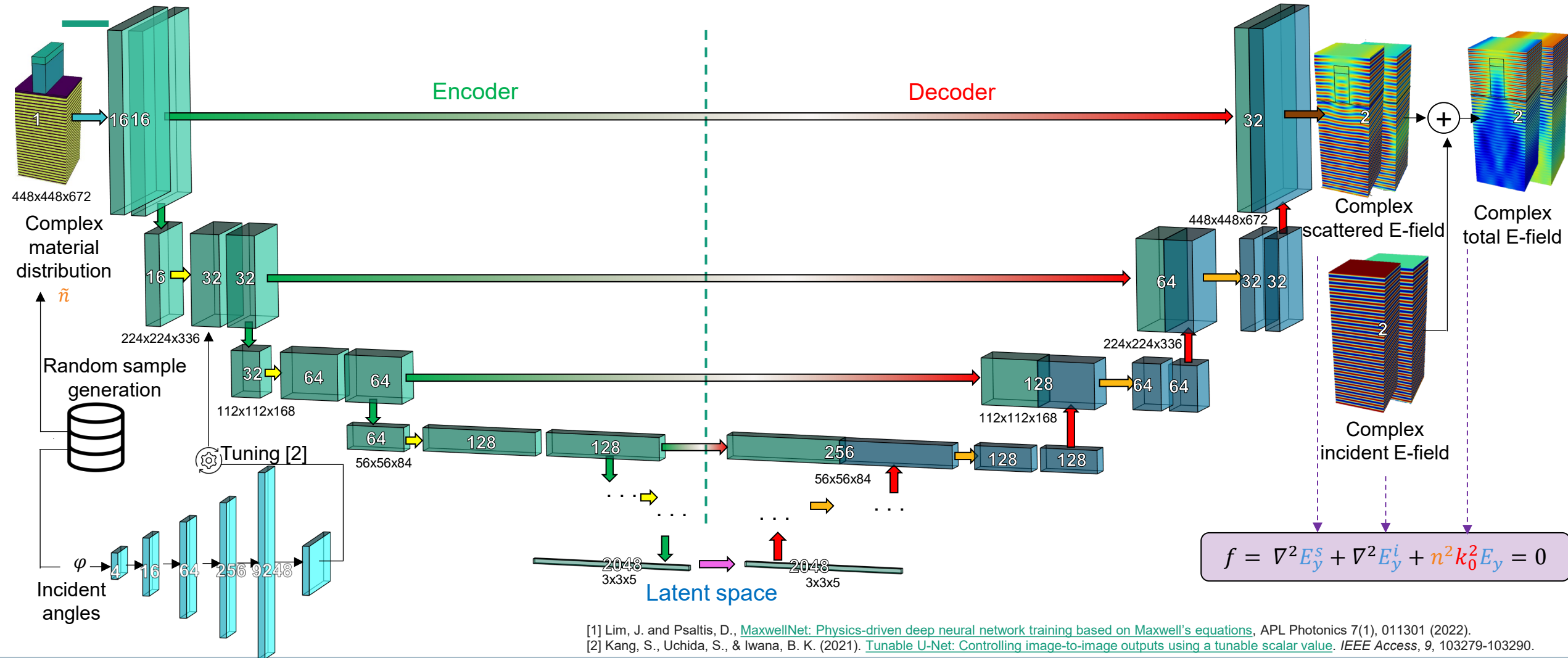
### Different material properties

- Absorber: TaBN, low-n low-k, low-n medium-k, etc.
- Multilayer: MoSi, RuSi, intermixing, etc.

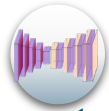
# 3D PINN



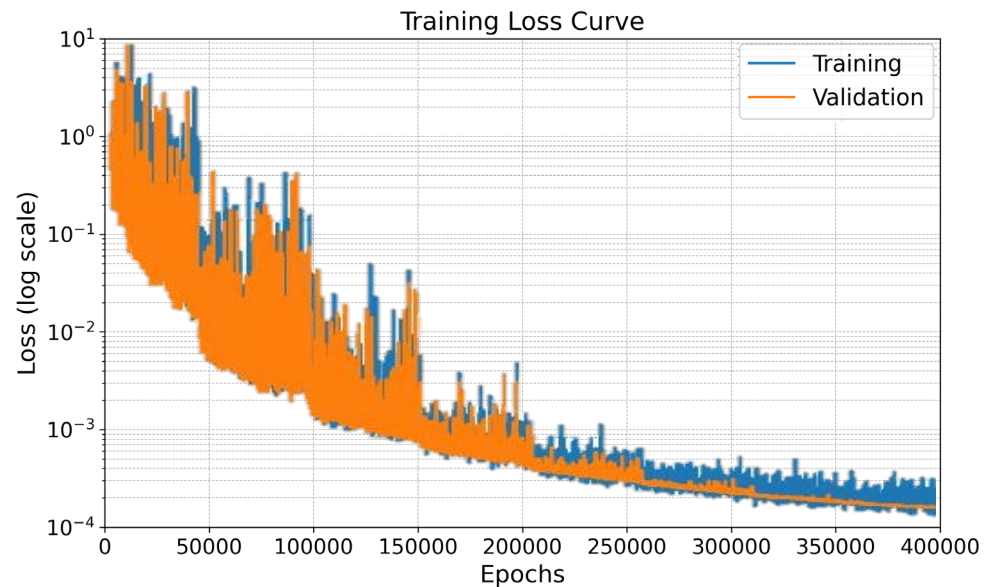
## U-Net architecture [1]



# 3D PINN



## Training parameters



- Good **convergence** behavior.
- **Speedup** with respect to Waveguide solver: up to  $\times 10000$ .

Table 1: Parameterization ranges.

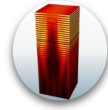
	<b>2D</b>
Absorber thickness, nm	[52, 80]
Feature size (wafer), nm	[20, 30]
Incident angle, °	[0, 15]
Azimuthal angle, °	[-25, 25]

Table 2: Time evaluation.

	<b>2D</b>	<b>3D</b>
Training time	~1-2 days	~7-8 days
Inference time	~1.10 ms	~100 ms

# Near-field prediction

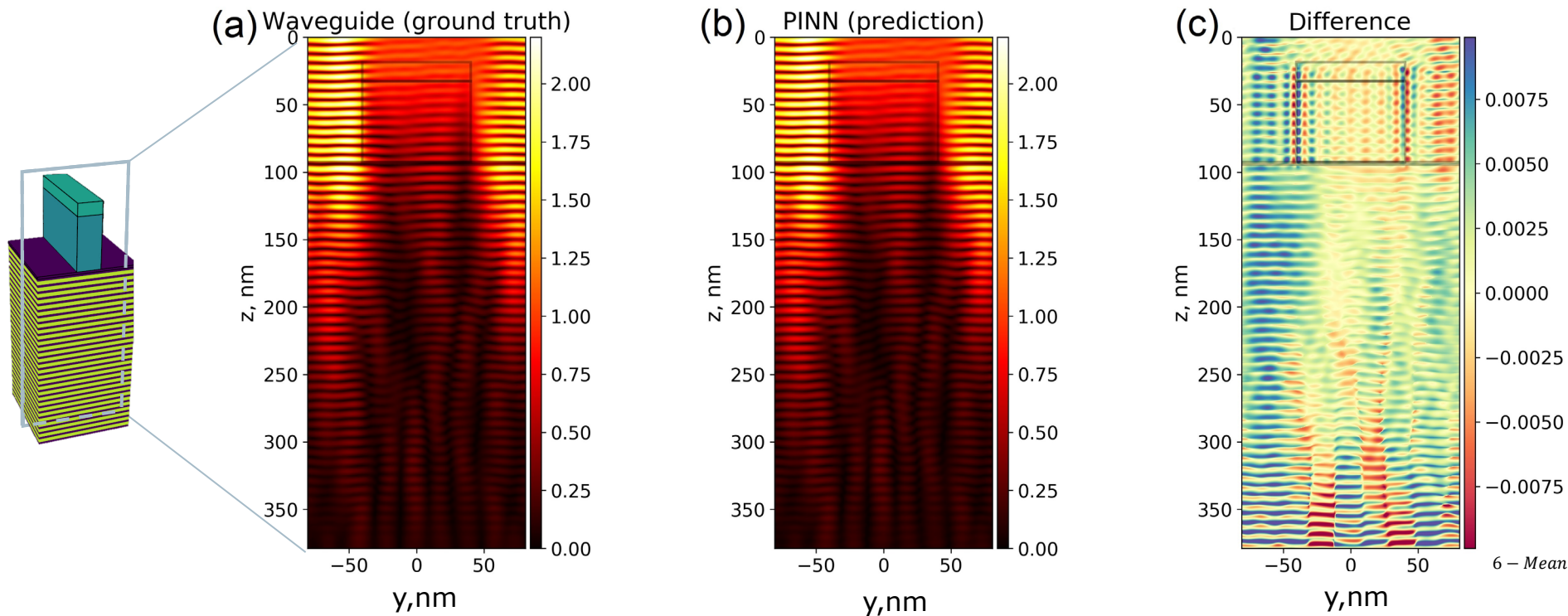
## Accuracy evaluation



### Input parameters:

- $\varphi = 6^\circ$
- Feature type: line (hor)
- Feature size: 20 nm
- Pitch: 40 nm
- Multilayer (ML): 40xMoSi

- In contrast to other machine learning approaches, PINN is able to accurately predict the **near field** and **learn physics**.
- PINN accurately captures the physics and optical effects such as mask **shadowing** effects, **partial penetration** of EUV light into the reflective ML, and **phase deformation** by the EUV absorber.



### PINN accuracy:

$$MAPE_{z=0}^6 = 0.18\%$$

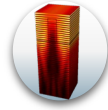
$$MAPE = 0.91\%$$

$$RMSE^7 = 4.1E - 3a.u$$

6 – Mean absolute percentage error:  $MAPE = \frac{100\%}{N} \sum_{i=1}^N \left| \frac{E_{ref} - E_{pred}}{E_{ref}} \right|$

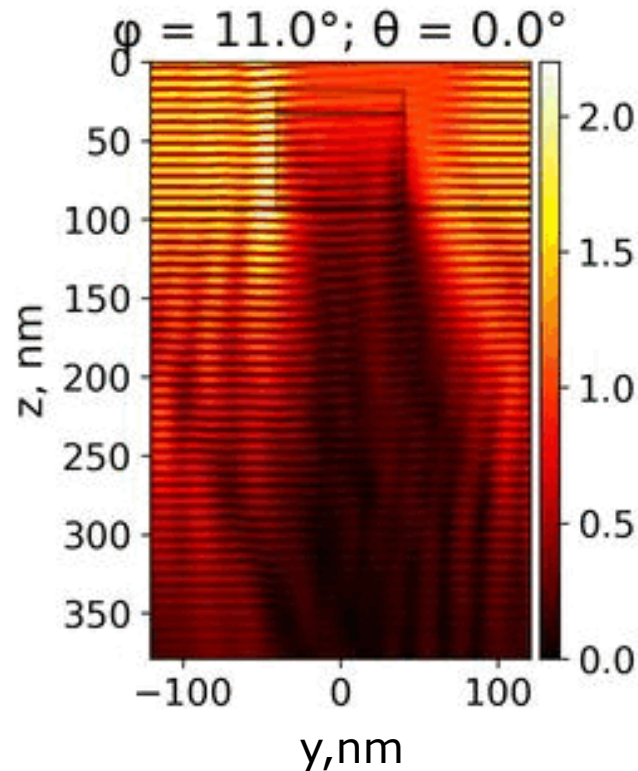
7 – Root mean squared error:  $RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (E_{ref} - E_{pred})^2}$

# Near-field prediction



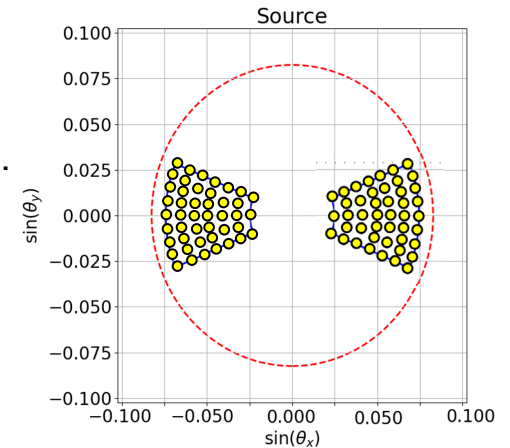
## Parameterization

- U-Net architecture makes PINN well-positioned for large-scale and high-dimensional problems due to **parameter sharing via filter-based convolution operations**.
- Differently from numerical solvers, once trained, generalized PINN can simulate light scattering in **a few tens of milliseconds without re-training** and **independently of problem complexity**.



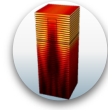
PINN model parameterized towards illumination:

- The Hopkins approach cannot be used for correct EUV imaging simulation.
- The advantage of a trained PINN is that the imaging simulation time is almost **independent** from the number of used noHopkins points.

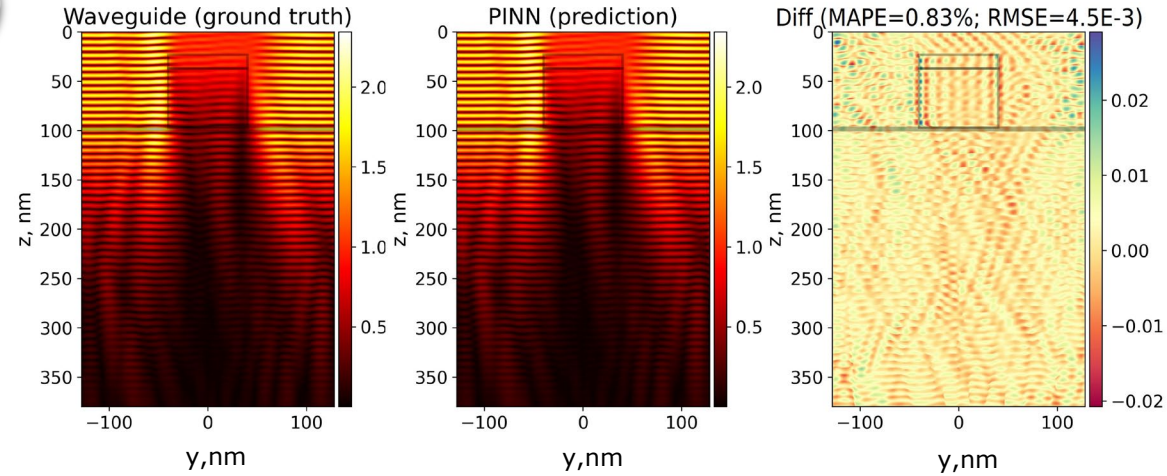


# Far-field prediction

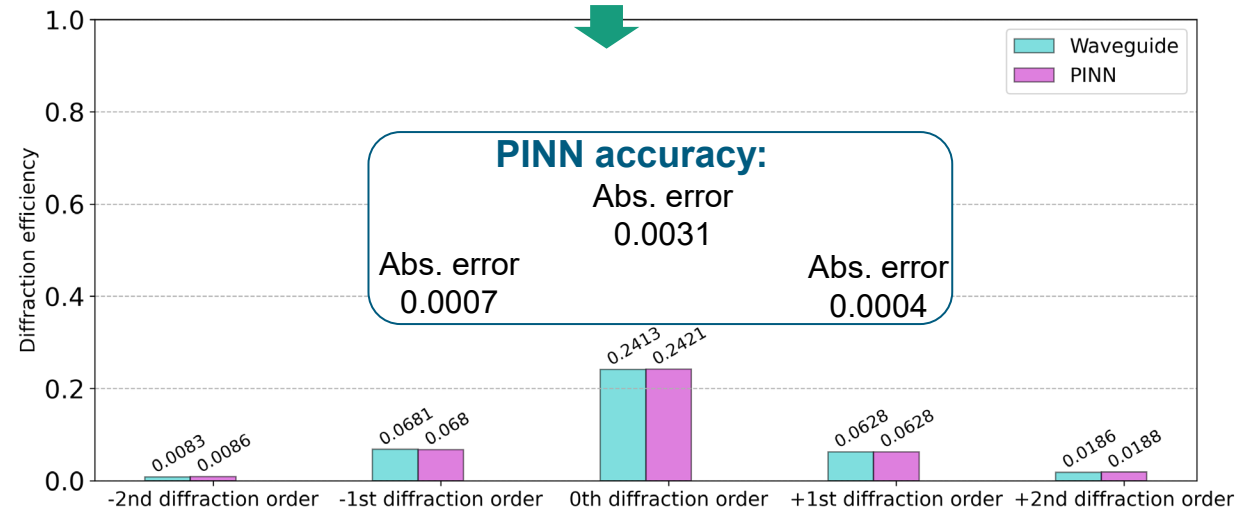
## Accuracy evaluation



- Input parameters:**
- $\varphi = 6^\circ$
  - Feature type: horizontal line
  - Feature size: 20 nm
  - Pitch: 64 nm
  - Multilayer: 40xMoSi

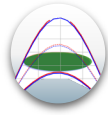


Near-to-far-field transformation (FT)



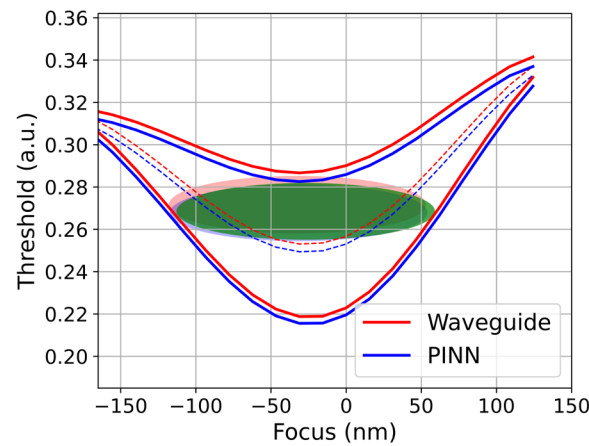
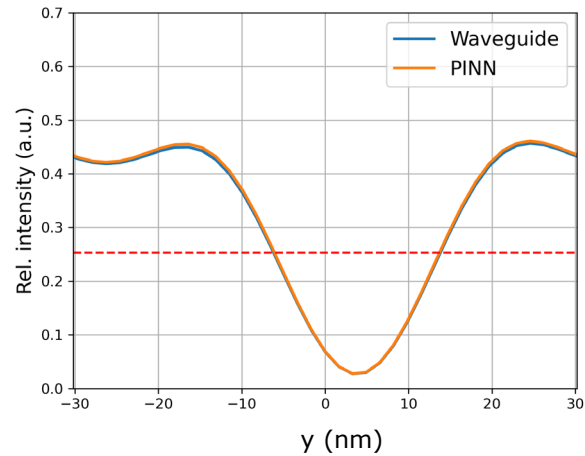
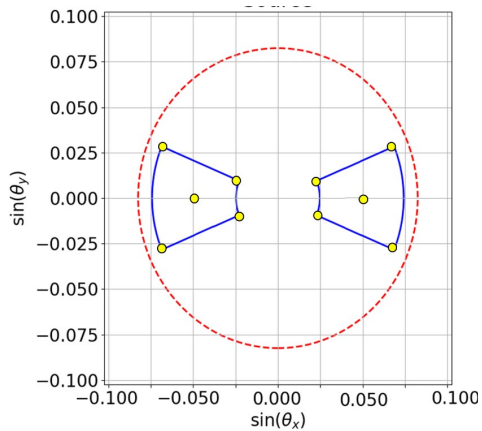
# Lithographic imaging

## Relevant metrics

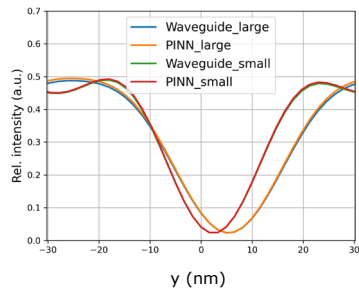


Pitch = 64 nm	
Projection:	
▪ NA = 0.33	
Illumination:	
▪ Inner pole radius $\sigma_{in}$	= 0.30
▪ Outer radius $\sigma_{out}$	= 0.90
▪ Opening angle	= 45°
▪ noHopkins point per pole	= 5

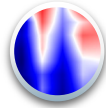
- The overlapping green area **almost completely covers** the ellipses of both process windows → sufficient PINN's accuracy in predicting lithographic process windows.



**PINN accuracy:**  
 $CD_{PINN} = 19.81$  nm (error 0.95%)  
 $NILS_{PINN} = 2.67$  (error 0.75%)



# Mask 3D effects



## 1. Non-telecentricity (nTC)

Pitch = 64 nm

Projection:

▪ NA = 0.33

Illumination:

▪ Inner pole radius  $\sigma_{in}$

= 0.30

▪ Outer radius  $\sigma_{out}$

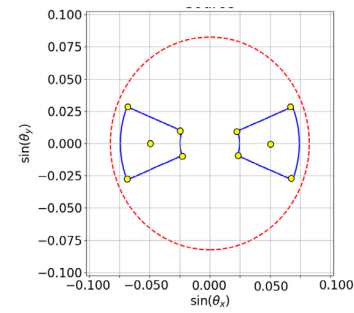
= 0.90

▪ Opening angle

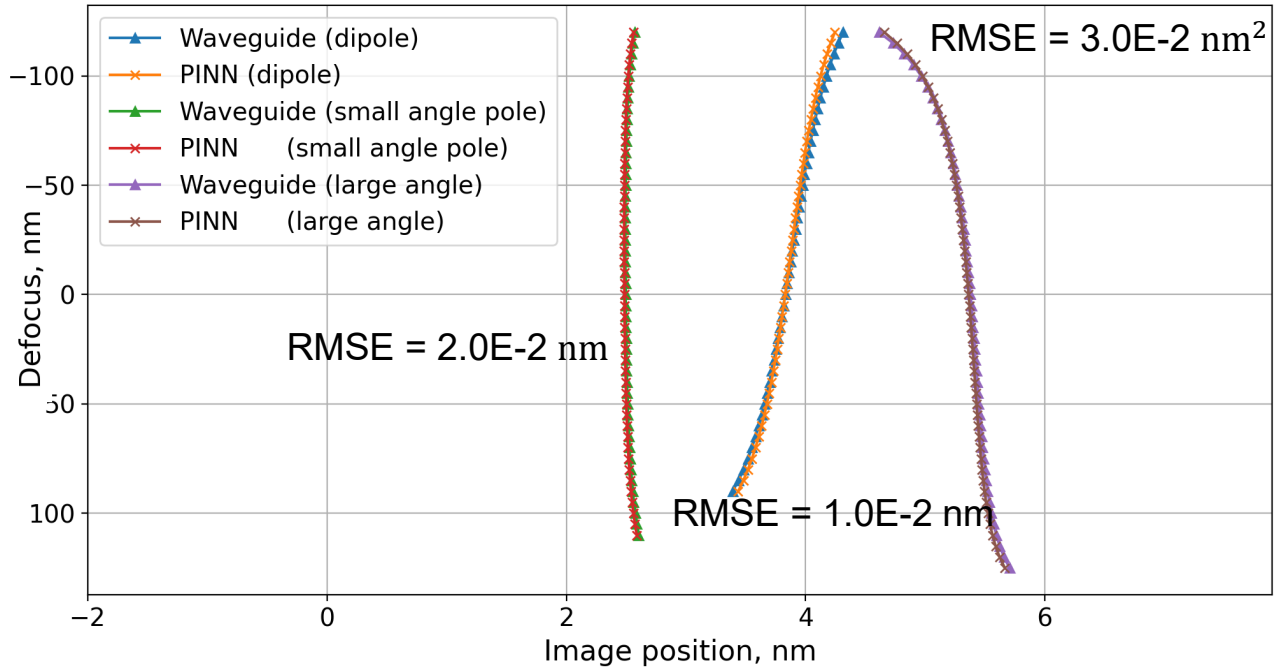
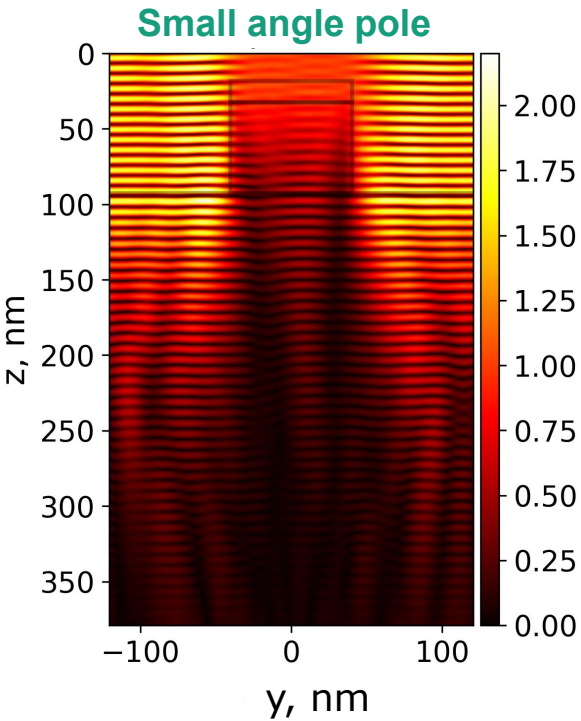
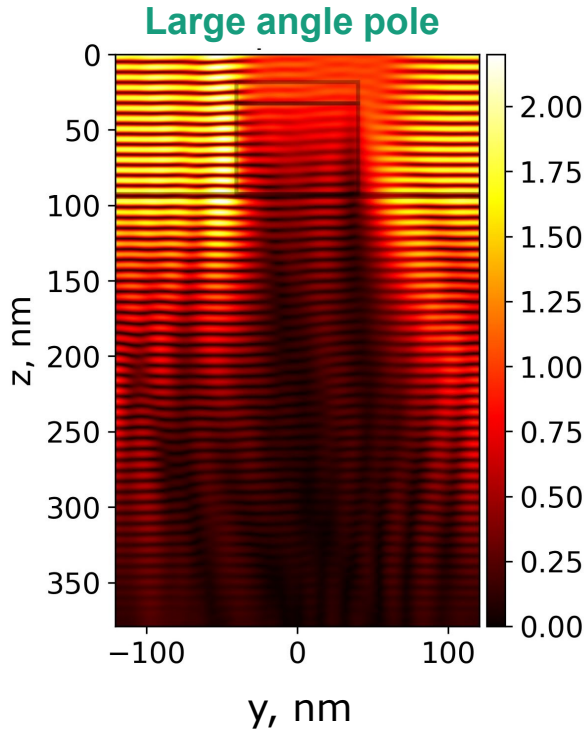
= 45°

▪ noHopkins point per pole

= 5



- Both 3D mask design and off-axis illumination contribute to **nTC error** → shifts of image position through focus (pattern placement errors).



**PINN accuracy:**  
 $nTC_{PINN} = 2.77 \text{ mrad}$   
 (error 0.72%)



# Mask 3D effects



## 2. Contrast fading

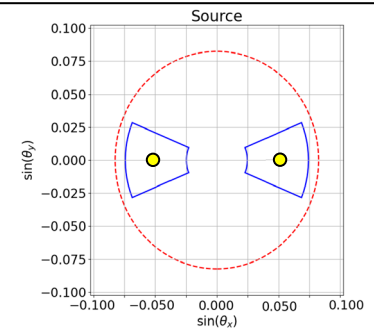
Pitch = 60 nm

Projection:

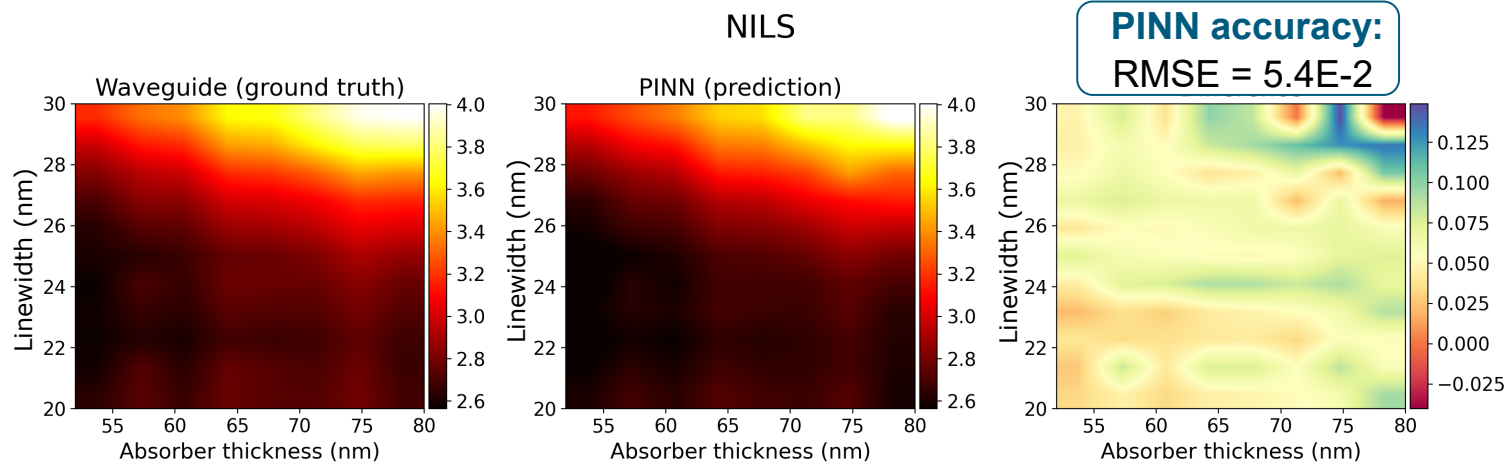
- NA = 0.33

Illumination:

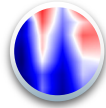
- Inner pole radius  $\sigma_{in}$  = 0.30
- Outer radius  $\sigma_{out}$  = 0.90
- Opening angle = 45°
- noHopkins point per pole = 1



- Shadowing causes a shift between images from left and right poles → superposition of shifted images causes **a drop of NILS**.
- PINN explores variations of image blur vs. physical parameters in a **short time**.
- PINN can predict both diffraction order balancing and shifts of image position → **improved image** contrast through optimization.



# Mask 3D effects



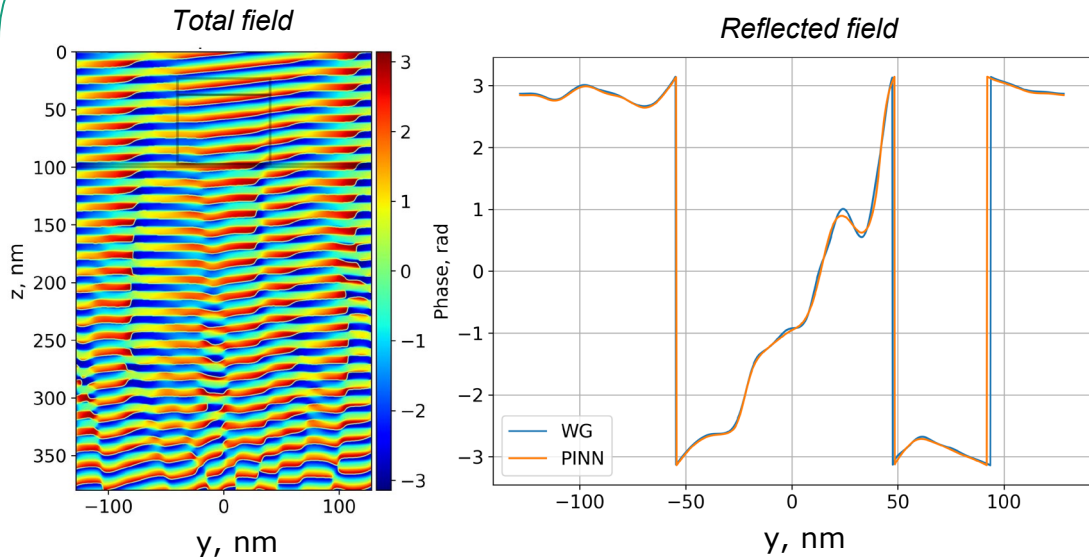
## 3.1 Shift of the best focus (BF)

Input parameters:

- $\varphi = 6^\circ$
- Feature type: line (hor)
- Feature size: 20 nm
- Pitch: 64 nm
- Multilayer: 40xMoSi

- Mask topography and the **phase distortion** in multilayer cause a shift of the BF position.
- PINN predicts correct phase shift between orders  $\rightarrow$  therefore it can predict best focus shift versus **physical parameters** (pitch, absorber thickness, feature size).

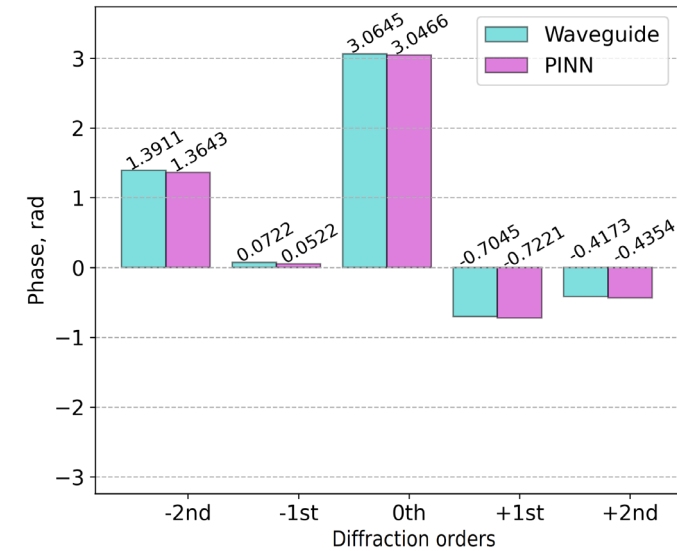
**Near field: phase deformation (i)**



**PINN accuracy:**

Phase:  $MSE = 1.8E-3 \text{ rad}^2$

**Far field: asymmetric diffraction behavior (ii)**



**PINN accuracy:**

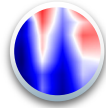
Between -1st/0th:

$\delta(\Delta\text{phase}) = 0.07\%$

Between 0th/+1st:

$\delta(\Delta\text{phase}) = 0.01\%$

# Mask 3D effects



## 3.2 Shift of the best focus

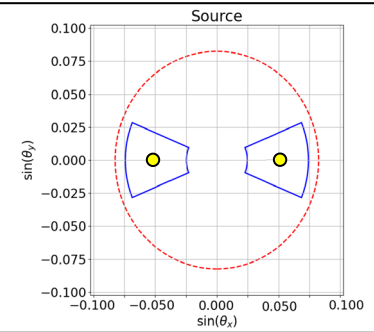
Pitch = 60 nm

Projection:

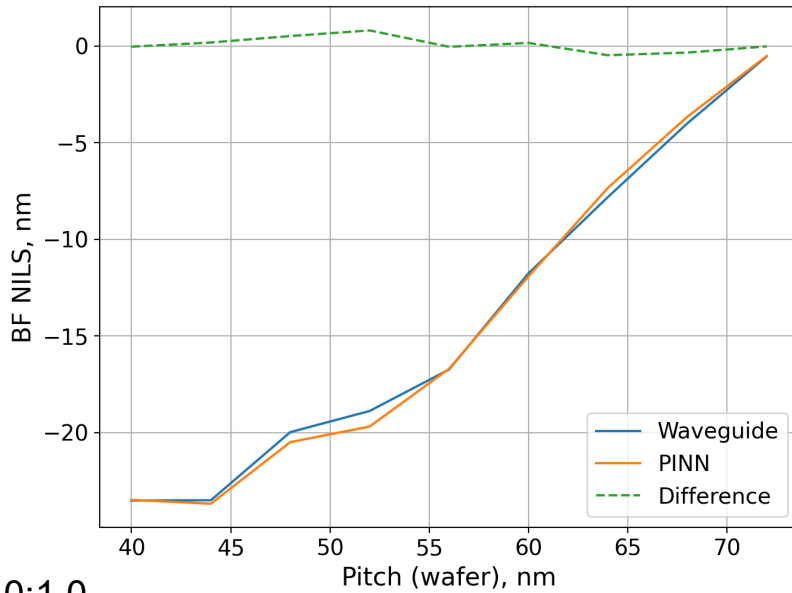
- NA = 0.33

Illumination:

- Inner pole radius  $\sigma_{in}$  = 0.30
- Outer radius  $\sigma_{out}$  = 0.90
- Opening angle = 45°
- noHopkins point per pole = 1



BF vs. Pitch



1.0:1.0

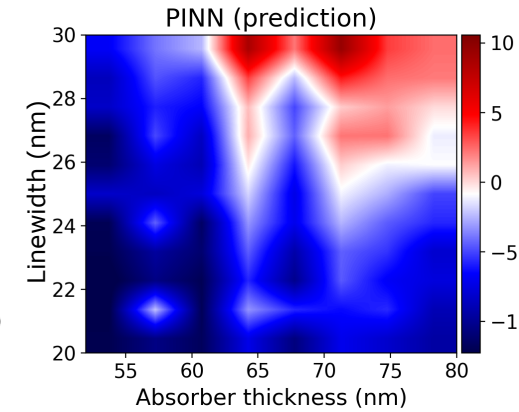
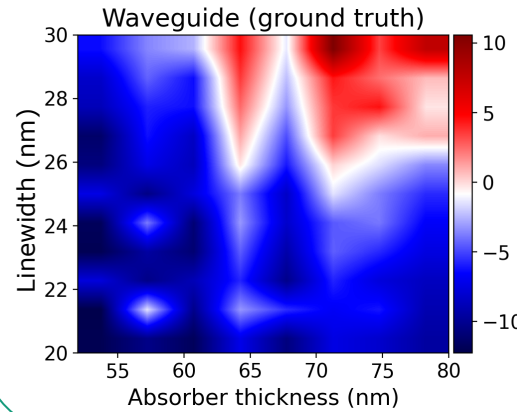
Duty ratio

1.0:3.6

PINN accuracy:

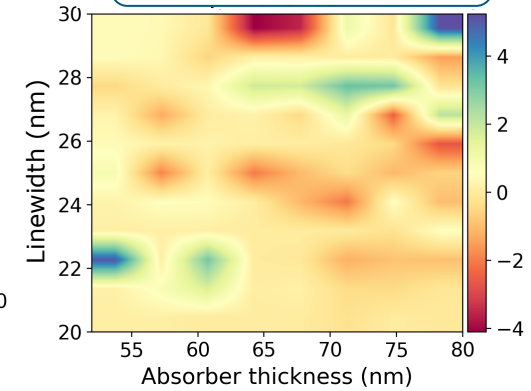
RMSE = 9.0E-3 nm

BF vs. Size/Absorber thickness



PINN accuracy:

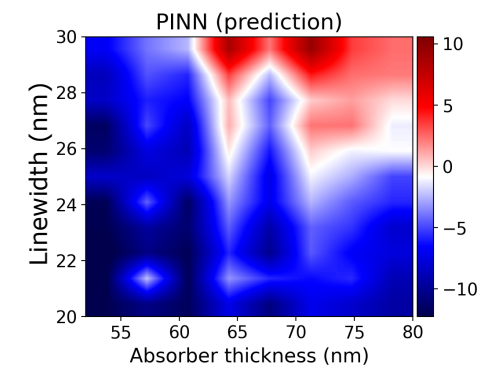
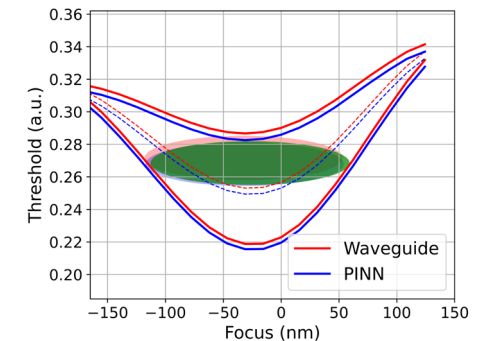
RMSE = 1.2 nm



- Trained PINN can predict BF versus absorber thickness, illumination and other settings in **short time**.
- PINN captures physical effects, such as the **swing behaviour** of BF versus absorber thickness variations.

# Summary

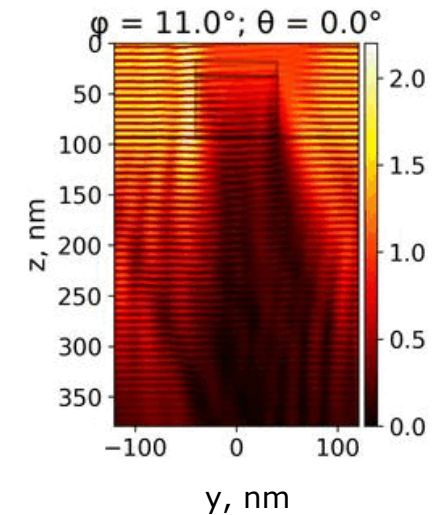
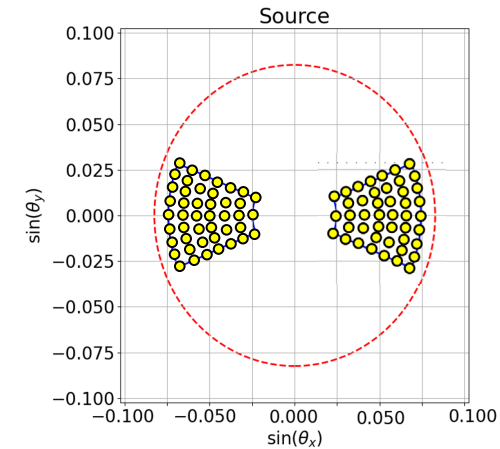
- For the first time the potential of PINN to simulate EUV light diffraction from typical reflective EUV masks was explored:
  - Good **convergence behaviour, high accuracy, and** stability.
  - Ability to **interpolate** and **generalize** across variations of EUV lithography-related parameters (illumination and mask geometries).
- PINN compared to other *machine learning* approaches:
  - is able to accurately simulate the near field.
  - learns given physics and accurately captures the optical and mask-induced 3D effects.
  - **NO experimental or rigorously simulated data** is required for training.
- PINN compared to rigorous *numerical solvers*:
  - Fast inference time (ms) → **significant speedup** (up to  $\times 10000$ ) w.r.t. to numerical solution.
  - Generalizability: light scattering simulation without re-training and independently of problem complexity.



# Outlook

## PINN for EUVL applications

- PINN-based solver, adapted for arbitrary illumination settings → imaging simulation time is almost **independent** from the number of used noHopkins points.
- Employing a vector formulation of the wave equation → investigate the ability of the PINN approach to predict the weak **polarization effects**.
- **Inverse design** → PINNs application in the OPC, SMO and ILT.



For any questions please contact: [vlad.medvedev@iisb.fraunhofer.de](mailto:vlad.medvedev@iisb.fraunhofer.de)

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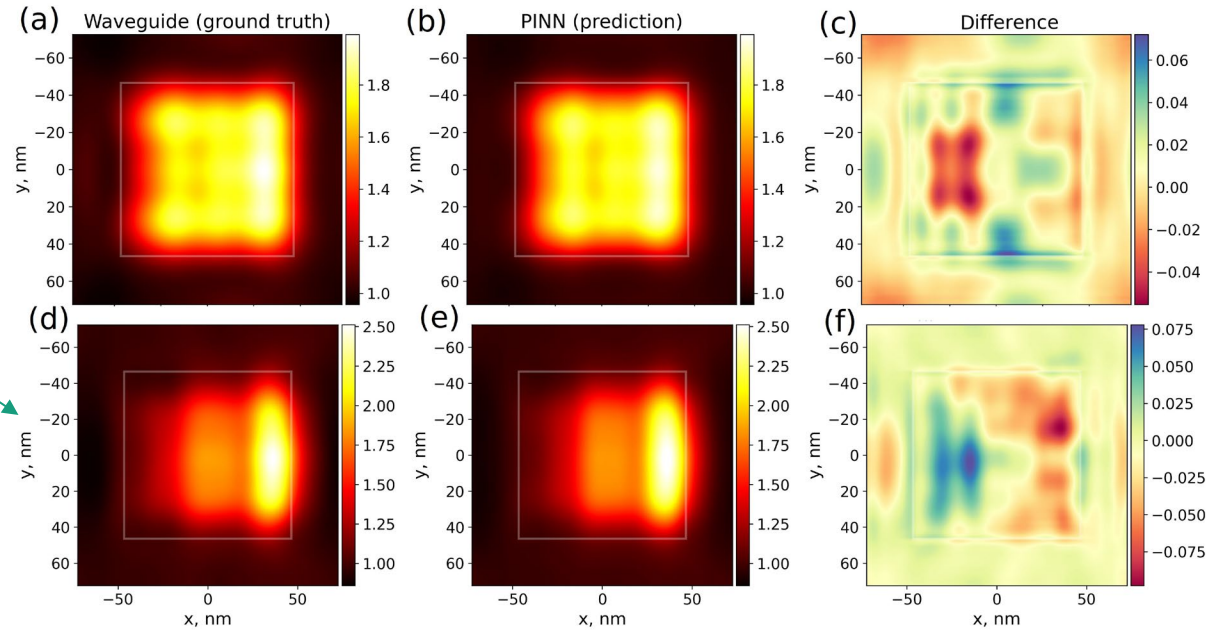
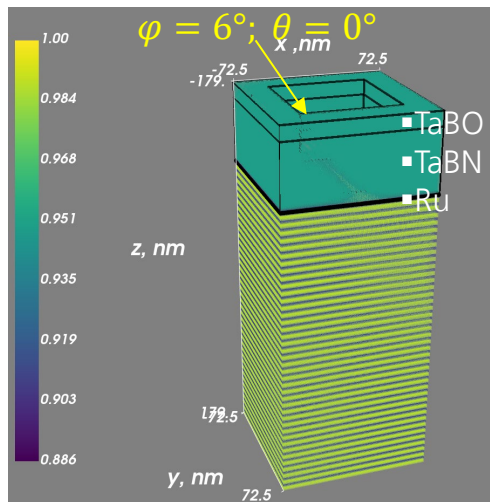
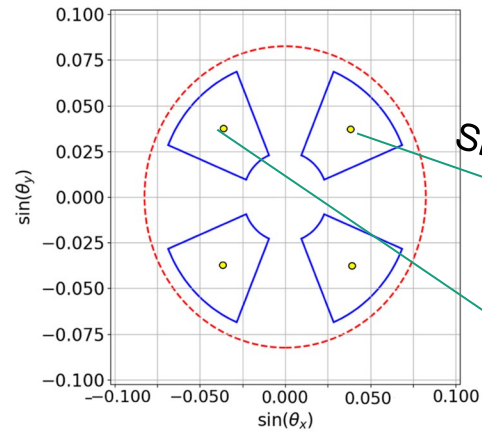
# Backup

# Simulation of 18 nm contact hole

## Near field evaluation

### Input parameters:

- $\varphi = 6^\circ$
- Feature type: contact hole
- Feature size (mask): 72 nm +biasing
- Feature size (wafer): 18 nm
- Pitch: 36 nm
- Multilayer (ML): 40xMoSi



**PINN accuracy:**

$MAPE_{z=0} = 0.91\%$

$RMSE = 1.2E - 2a.u$

$MAPE_{z=0} = 0.95\%$

$RMSE = 1.4E - 2a.u$

# Simulation of 18 nm contact hole

## Lithographic imaging

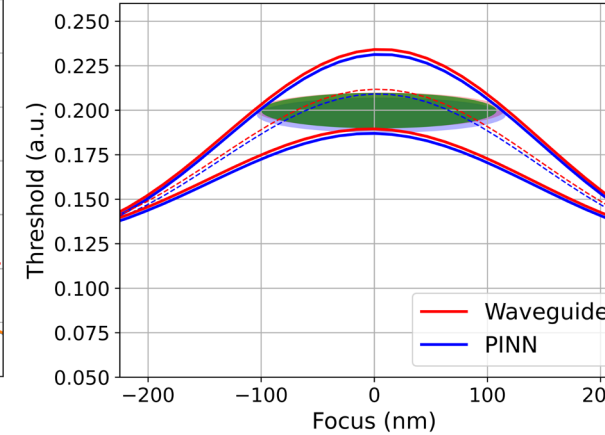
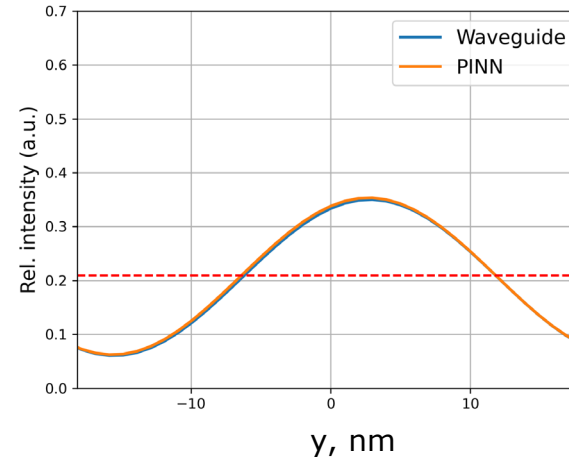
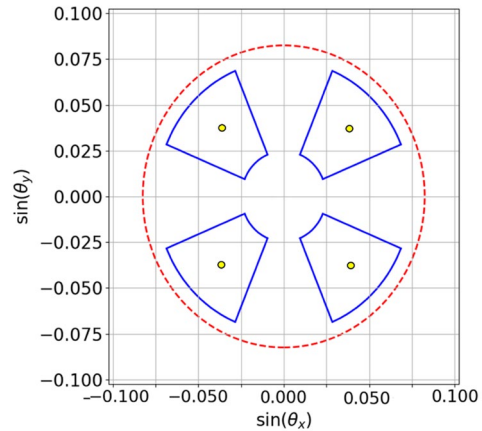
Pitch = 36 nm

Projection:

- NA = 0.33

Illumination:

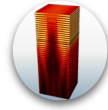
- Inner pole radius  $\sigma_{in}$  = 0.30
- Outer radius  $\sigma_{out}$  = 0.90
- Opening angle = 45°
- noHopkins point per pole = 1



Parameter	Waveguide method	PINN	Percentage error, %
CD, nm	18.00	18.21	1.17
NILS	2.13	2.14	0.47
Best focus NILS, nm	17.39	17.90	2.93
Depth of focus NILS, nm	163.56	159.67	2.37



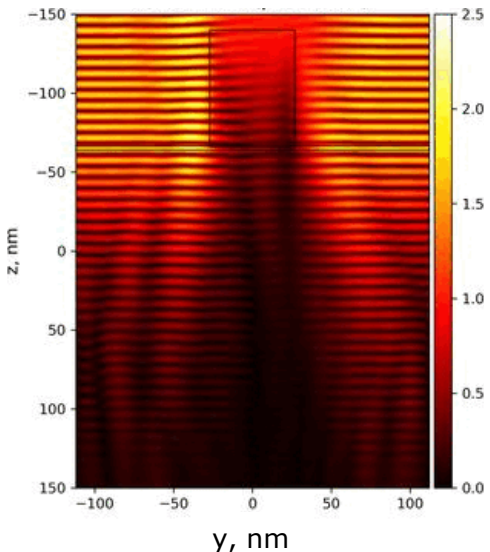
# Near-field prediction



## Parameterization

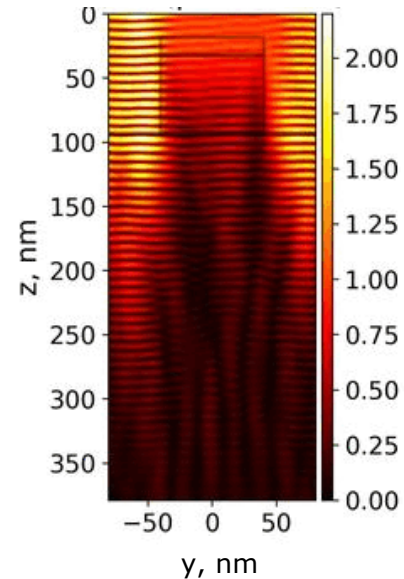
- U-Net architecture makes PINN well-positioned for large-scale and high-dimensional problems due to **parameter sharing via filter-based convolution operations**.
- Differently from numerical solvers, once trained, generalized PINN can simulate light scattering in **a few tens of milliseconds without re-training** and **independently of problem complexity**.

### Absorber geometry variations



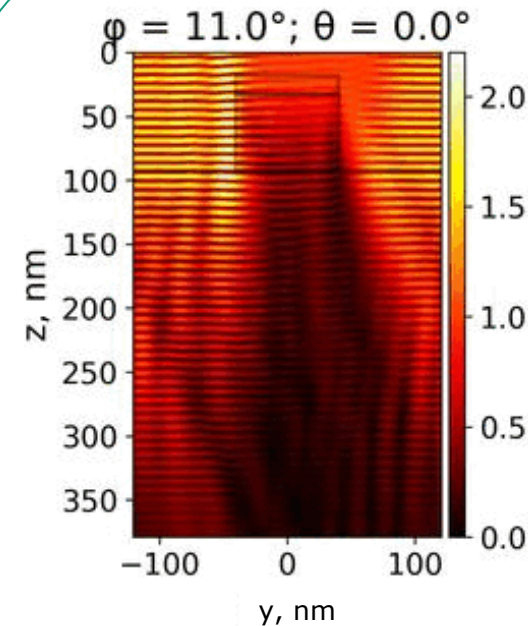
- Inverse problems.
- Topology optimization.

### Pitch variations



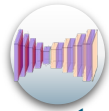
- Studying mask 3D effects.

### Illumination variations



- Partially coherent imaging simulations without the assumption of shift-invariance (noHopkins approach).
- Seamless integration with spectrum and domain decomposition methods.

# 3D PINN



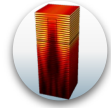
## Training parameters

Table 1: Model parameters

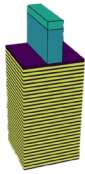
NetworkSpecs	
Type	Convolutional Neural Network
U-Net depth	[6...8]
Filter	16
Batch size	4
Learning rate	[1E-4 ... 3E-4]
Learning rate decay	Exponential; ×0.5 every 50000 epochs
Activation function	CELU
Optimization	Adam
GPU machine	2 x NVIDIA A100 80 Gb

# Far-field prediction

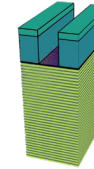
## Accuracy evaluation



Line

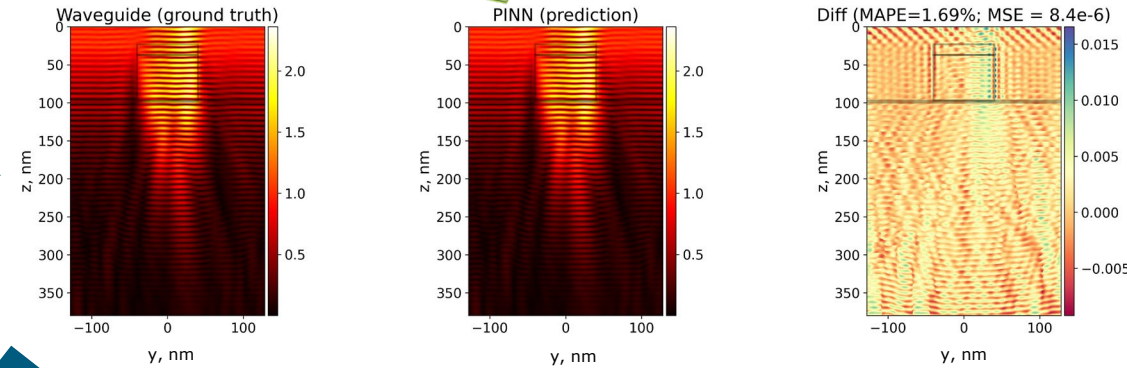
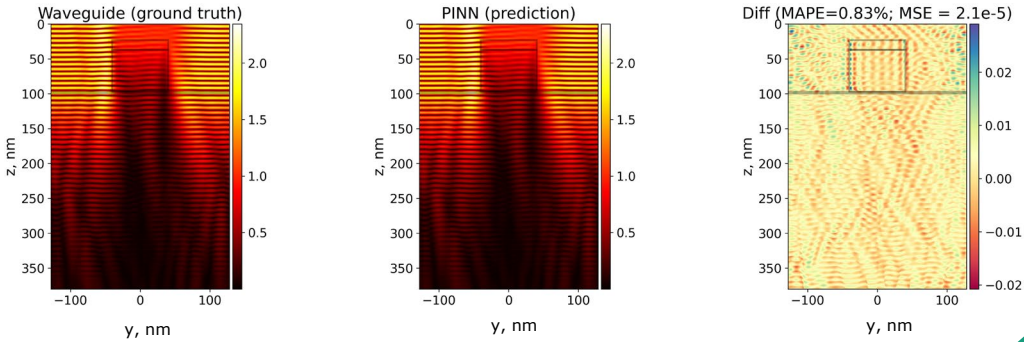


Space

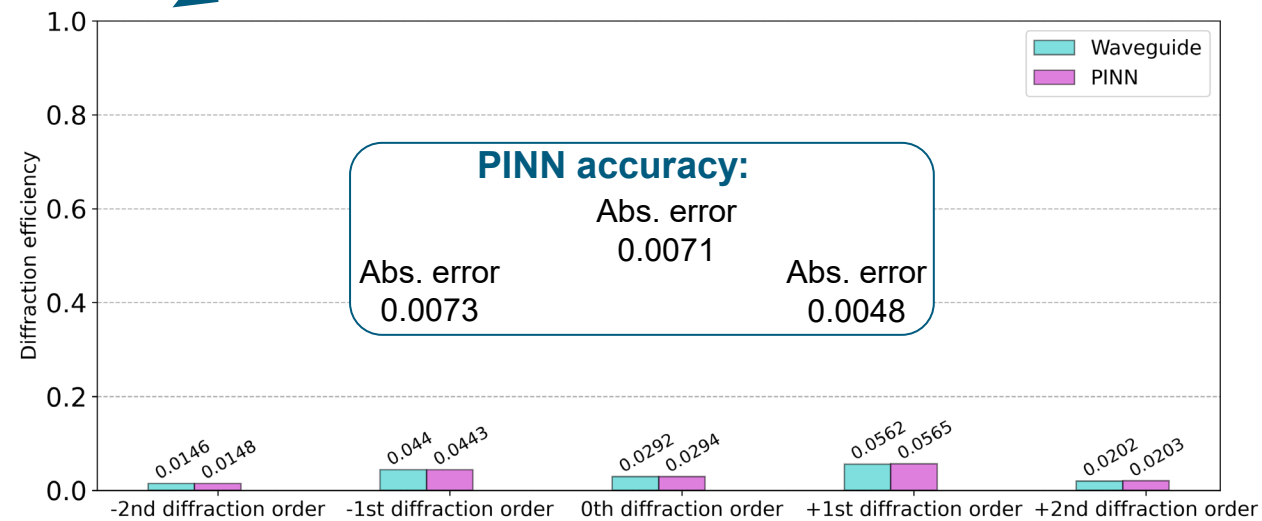
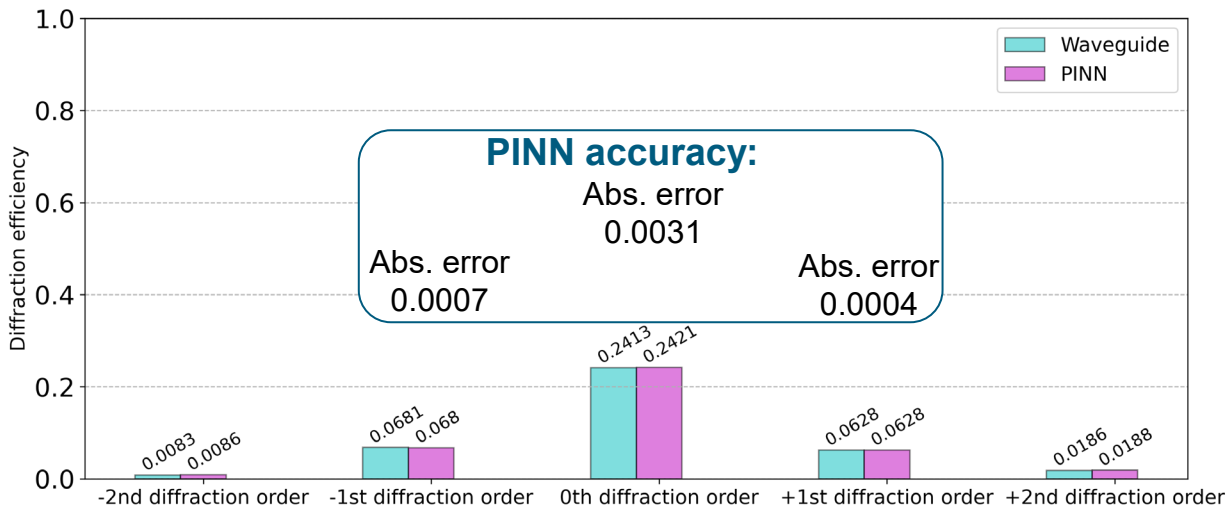


Input parameters:

- $\varphi = 6^\circ$
- Feature type: line/space (hor)
- Feature size: 20 nm
- Pitch: 64 nm
- Multilayer: 40xMoSi



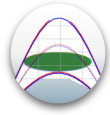
Near-to-far-field transformation (FT)



# Lithographic performance

## Relevant metrics

- The overlapping green area **almost completely covers** the ellipses of both process windows → sufficient PINN's accuracy in predicting lithographic process windows.

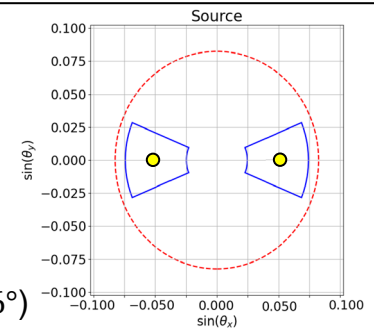


### Projection:

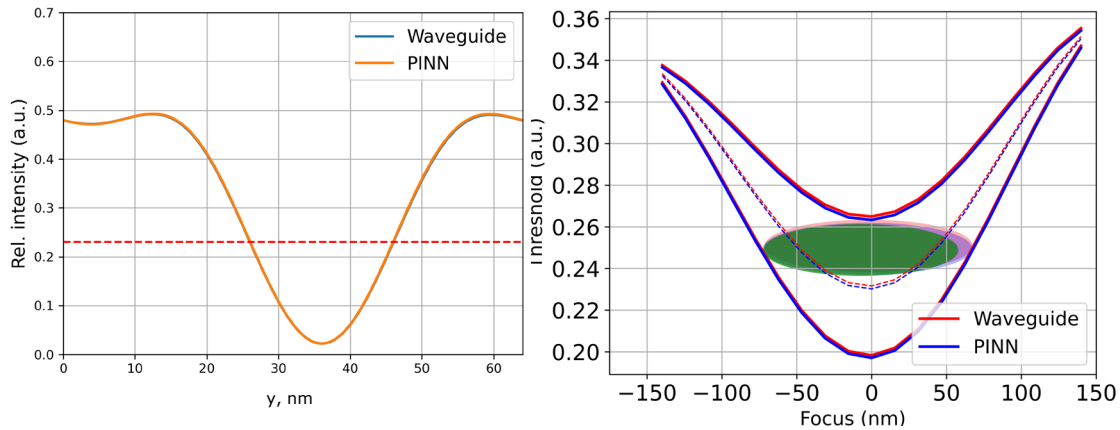
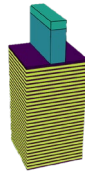
- NA = 0.33

### Illumination:

- Inner pole radius  $\sigma_{in}$  = 0.30
- Outer radius  $\sigma_{out}$  = 0.90
- Radial source point density = 20
- Tangential source point density = 70
- noHopkins point per pole = 1 ( $\varphi \pm 2.86^\circ$ )



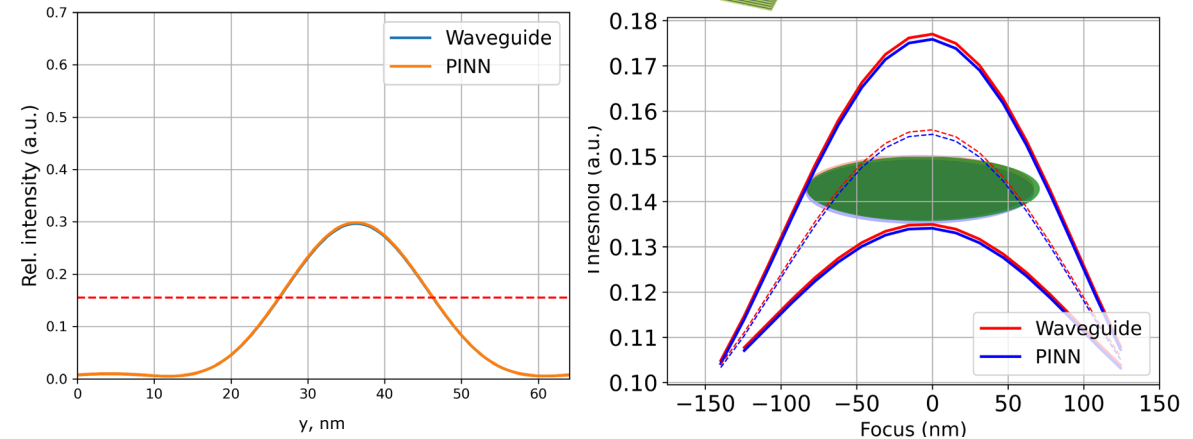
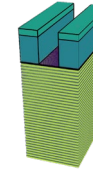
### Line



#### PINN accuracy:

$$CD_{PINN} = 19.92 \text{ nm (error 0.42\%)}$$

### Space



#### PINN accuracy:

$$CD_{PINN} = 20.09 \text{ nm (error 0.47\%)}$$